### **Application**

1. Speed = 
$$\frac{\text{Distance}}{\text{Time}}$$

- 2. Area of figures
- 3. Flow rate x time = volume of water
- 4. Number or ages

**e.g.** The hypotenuse of a right triangle is 25 cm. The difference between the lengths of the other two sides of the triangle is 5 cm. Find the lengths of these sides. **Sol.** Shorter side = x cm, longer side = (x + 5) cm.

hypotenuse = 25 cm by pythagoras Theorem

$$x^{2} + (x + 5)^{2} = 25^{2}$$
  
 $x^{2} + 5x - 300 = 0$ 

$$(x + 20)(x - 15) = 0$$

This gives x = 15 or x = -20.

We reject x = -20 and take x = 15.

Thus, length of shorter side = 15 cm.

Length of longer side = (15 + 5) cm, i.e., 20 cm.

### Factorisation method

In this method ( $ax^2 + bx + c$ ) be expressible as the product of two linear expression , say (px + q) and (rx + s), where p, q, r are real numbers such that p  $\neq 0$  and  $r \neq 0$ Then  $ax^2 + bx + c = 0 \Rightarrow (px + q) (rx + s) = 0$  $\Rightarrow (px + q) = 0$  or (rx + s) = 0 $\Rightarrow x = -\frac{q}{p}$  or  $x = -\frac{s}{r}$ 

# Quadratic Equations

An equation of the form  $ax^2 + bx + c = 0$ , where a,b,c are real numbers and  $a \neq 0$ , is called a quadratic equation in x.

Solution or Roots of Quadratic Equation A real number  $\alpha$  is called a root of the quadratic equation  $ax^2 + bx + c = 0$ ,  $a \ne 0$  if  $a\alpha^2 + b\alpha + c = 0$ 

# Method of finding solution

### Completing the square method

$$ax^{2} + bx + c = 0, a \neq 0.$$

$$x^2 + \frac{b}{a}x + \frac{c}{a} = 0$$

$$x^2 + \frac{b}{a}x = -\frac{c}{a}$$

$$x^2 + 2\left(\frac{b}{2a}\right)x + \left(\frac{b}{2a}\right)^2 = \left(\frac{b}{2a}\right)^2 - \frac{c}{a}$$

$$\left(x + \frac{b}{2a}\right)^2 = \left(\frac{b}{2a}\right)^2 - \frac{c}{a}$$

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2 - 4ac}{4a^2}$$

$$x + \frac{b}{2a} = \pm \sqrt{\frac{b^2 - 4ac}{4a^2}}$$

Obtain the values of x by shifting the constant term  $\frac{b}{2a}$  on RHS

#### Nature of roots

 $ax^2 + bx + c = 0$ , where  $a \neq 0$ D =  $(b^2 - 4ac)$ . and the roots are given by

$$\alpha = \frac{-b + \sqrt{D}}{2a}$$
 and  $\beta = \frac{-b - \sqrt{D}}{2a}$ 

Case - I

When D > 0, roots are real distinct and given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} \text{ and } \beta = \frac{-b - \sqrt{D}}{2a}$$

Case - II

When D = 0, roots are real and equal and roots are given by

$$\alpha = \beta = -\frac{b}{2a}$$

Case - III

When D < 0, roots are not real.

## Quadratic formula:

for  $ax^2 + bx + c = 0$ ,

$$D = b^2 - 4ac$$

$$x = \frac{-b \pm \sqrt{D}}{2a}$$

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